Assignment 5

due Monday, November 15, 2010

1. Exercise 13.1-6, p 312. [6 points]
2. Give a binary tree which can be colored as a red-black tree but which is not an AVL tree. [4 points]
3. Do (i) exercise 13.3-2, p 322, (ii) then insert 35, 37, 22, (iii) and finally delete 19 and 31. Show the tree after each phase (and more if you wish). [8 points]
4. Let T be a tree storing 100,000 items. What is the worst case height of T in the following cases?
   (a) T is an AVL tree
   (b) T is a (2,4) tree
   (c) T is a red-black tree
   (d) T is a binary search tree
   [8 points]
5. Exercise 18.2-1, p 497, but change the minimum degree from 2 (which would be a (2,4)-tree) to 3. [6 points]
6. Let T and U be two red-black trees storing n and m items, respectively, such that any item in T has a key less than the keys of all items in U. Describe an O(lg n + lg m) method for joining the trees into a single tree that stores all the items in T and U. The original T and U may be be destroyed in the process. [8 points]
7. Show how to use a heap to find the kth largest of a set of n elements in O(n + k log n) time [4 points]

Total: 44 points

Notes:

- Q1: As usual, internal node means actual node and external node means a null.
- Q2: Of course, here we are just considering the shape of the tree. You are to show a tree which could be colored as a RB tree but is too out of balance to be an AVL tree.
- Q6: Try to adapt the solution of the same (2,4)-tree problem. This is essentially exercise 13-2 from the text.
- Q7: Use the fact that heap-build is O(n) and heap-delete is O(log n).